Inflation Targeting in Brazil: Constructing Credibility under Exchange Rate Volatility

1. Introduction

This paper assesses the inflation-targeting regime in Brazil adopted in June 1999, examining the main challenges it has faced over its first three and half years. In particular, we stress two important challenges that are also common in other emerging market economies: construction of credibility, and high exchange rate volatility.

The inflation-targeting mechanism has played a key role in macroeconomic stabilization in Brazil. In spite of large inflationary shocks, the inflation rate has been maintained at a low level. Exchange rate depreciations in 2001 and 2002 were stress tests for the regime. In particular, in 2002 monetary policy faced a confidence crisis in the future performance of the Brazilian economy and an increase in risk aversion in international markets. Rollover rates of domestic public debt securities diminished considerably, and the Brazilian economy experienced a "sudden stop" in capital inflows to the country, generating a significant nominal depreciation of the exchange rate.

Inflation targeting in emerging market economies has been a more challenging task than in developed economies. The conduct of monetary policy has to build credibility and reduce inflation rate levels, and simultaneously deal with a greater vulnerability to shocks. In fact, one basic task of the Central Bank of Brazil has been to build credibility as a monetary authority committed to price stability in the context of large inflationary shocks. This requires actions consistent with the inflation-targeting framework combined with high levels of transparency and communication with the public.¹ Furthermore, it is expected that private agents' inflation expectations do not depart way from the targets without converging to them in a certain time horizon. We present some evidence on: i) the behavior of the central bank; ii) the behavior of private agents' expectations; iii) change in inflation dynamics; and iv) exchange rate volatility and pass-through.

Specifically, we estimate the central bank's reaction function, and find that monetary policy has been reacting strongly to inflationary pressures. In particular, the Central Bank reacts to inflation expectations, giving evidence that the monetary policy is conducted on a forward-looking basis.

We show that private sector inflation expectations did not depart significantly from the country's inflation targets until September 2002, even when faced with inflationary shocks. We present evidence that the inflation targets have worked as an important coordinator of expectations. The end of 2002 and beginning of 2003 in turn represents a period dominated by uncertainties concerning the future conduct of economic policy. We also find some evidence of a change in inflation dynamics, namely a reduction in the degree of inflation persistence, which however seems to have shown some signs of resurgence at the end-2002. We also stress the significant inflationary pressures stemming from exchange rate volatility. We estimate the pass-through from exchange rate changes to the inflation rate using a VAR estimation, showing the higher pass-through for "administered or monitored" prices.

The following section presents an overview of the first three and half years of inflation targeting. Section 3 assesses the different challenges for the inflation-targeting regime. Section 4 deals with exchange rate volatility. A final section concludes the paper.

2. Overview of the first three and half years of inflation targeting

Macroeconomic policy in Brazil over the past three and half years has consisted of three basic elements: a floating exchange rate regime, sound fiscal policy, and inflation targeting. The

¹ For the importance of transparency and communication, and an assessment of inflation targeting in emerging market economies, see Fraga, Goldfajn, and Minella (2003).

current inflation-targeting regime was adopted in mid-1999, after the currency was floated in January of the same year. In the first two years, annual inflation rates met their targets, having absorbed the initial impact of the exchange rate depreciation in 1999. The successful transition was supported by a considerable fiscal improvement, a shift in the primary (non-interest) fiscal balance of the consolidated public sector from roughly zero in 1998 to a surplus of 3.23% of GDP in 1999, 3.51% in 2000, 3.68% in 2001, and 3.9% in 2002.

Figure 1 shows actual inflation and the targets for 1999-2002. The inflation rate is measured by a consumer price index, the IPCA. Brazil's inflation targeting regime includes tolerance intervals around the central inflation targets. From 1999 to 2002, the tolerance intervals were 2 percentage points above and below the central target (for 2003 and 2004 the intervals were enlarged to 2.5 percentage points). The inflation rate was 8.9% and 6.0% for targets of 8% and 6% in 1999 and 2000, respectively.



However, in 2001 and 2002, several external and domestic shocks hit the Brazilian economy with significant impacts on inflation. The inflation rate reached 7.7% in 2001, 1.7 p.p. above the target's upper tolerance interval, and 12.5% in 2002, more than 5 points above the upper limit.² In 2001, a domestic energy crisis, the deceleration of the world economy, the September 11 terrorist attacks in the United States, and the Argentine crisis generated strong pressures on the exchange rate. In 2002, a further sharp depreciation was driven by increased risk aversion in international capital markets, and mainly by a confidence crisis related to uncertainties about the future Brazilian macroeconomic policies under a new government. Rollover rates of domestic public debt securities diminished considerably, and the Brazilian economy experienced a "sudden stop" in capital inflows to the country, generating a significant nominal depreciation of the exchange rate. The country risk premium rose from 750 basis points in April 2002 to a peak of 2,400 basis points at the end of September. Figure 2 shows the level of the exchange rate since 1998. The exchange rate (measured in units of local currency per dollar) rose 20.3% and 53.5% in 2001 and 2002, respectively (equivalent to a depreciation of the domestic currency of 16.9% and 34.8%). In addition to the impacts of the exchange rate depreciation, the energy crisis from 2001 to the beginning of 2002, and the deregulation of the domestic market for oil by-products also led to direct inflationary pressures.

 $^{^{2}}$ The reasons for the non-fulfillment of the targets in 2001 and 2002 were explained in open letters of the Governor of the Central Bank of Brazil to the Minister of Finance, available at www.bcb.gov.br.

Figure 2 Exchange Rate Level (R\$/US\$) - 1998:01- 2002:12 (Monthly Average)



Monetary policy has been faced with an important change in relative prices that has pushed up the overall inflation rate. The administered by contract or monitored prices – administered prices, for short – have increased by substantially more than the other prices – market prices, for short. Considering the period since the start of inflation targeting in Brazil, the ratio of administered prices to market prices has increased 31.4% (1999:7 - 2003:2). The administered prices are defined as those that are relatively insensitive to domestic demand and supply conditions or that are in someway regulated by a public agency.³

The dynamics of administered prices differ from those of market prices in three ways: i) dependence on international prices in the case of oil by-products; ii) greater pass-through from the exchange rate;⁴ and iii) stronger backward-looking behavior.⁵

Using the structural model of the Central Bank⁶ and information concerning the mechanisms for the adjustment of administered prices, it is possible to estimate the contribution for the inflation rate stemming from exchange rate pass-through, inflation inertia from the previous year, and inflation of administered prices and market prices that is not explained by the exchange rate pass-through and the mentioned inertia. Table 1 shows the estimated values for 2001 and 2002. In 2001, 38% of the inflation rate can be explained by the depreciation of the exchange rate, whereas for 2002 the contribution of the exchange rate stood at 46%.

In 2001 and 2002, the Central Bank aimed at minimizing the potential inflationary effects of the different shocks, mainly the exchange rate depreciation and the increase in administered prices. The main goal of monetary policy was to limit the propagation of the shocks to the other prices of the economy. Figure 3 presents the path of the basic interest rate – the Selic rate – controlled by the Central Bank. Between March and July 2001, the Central Bank raised the interest rate significantly (375 b.p.), interrupting the downward trend observed previously. Some improvement in the macroeconomic context at the beginning of 2002 allowed some reduction in the interest rate, interrupted by the inflationary pressure coming from the exchange rate depreciation.

³ The group includes, among others, oil by-products, fixed telephone fees, residential electricity, and public transportation. The aggregate weight of administered prices in the IPCA was 28.0% in December 2002.

⁴ There are three basic links: i) the price of oil by-products for consumption depends on international oil prices denominated in domestic currency; ii) part of the resetting of electricity rates is linked to changes in the exchange rate; and iii) the contracts for price adjustments for electricity and telephone rates link these adjustments, at least partially, to the General Price Index (IGP), which is more affected by the exchange rate than the consumer price indexes.

⁵ Electricity and telephone rates are generally adjusted annually, and the contractual clauses usually stipulate that adjustments should be based on a weighted average of the past change of the IGP price index and the exchange rate.

⁶ For an overview of the structural model, see Bogdanski *et. al.* (2000). Using the aggregate supply curve, which relates current market price inflation to the expected and past headline inflation, output gap, and exchange rate change, we estimate the contributions of the exchange rate pass-through and of inertia from the previous year to the market prices. For the administered prices, the estimation depends on the criteria used for the price adjustment of specific items.

Table 1
Contributions for Inflation: 2001-2002.
(In percentage points and in percentage contribution)

	200	1	2002		
Item	Contributions inPercentagepercentage pointscontribution		Contributions in percentage points	Percentage contribution	
Market Price Inflation Excluding Exchange Rate Pass-Through and Inertia	2.4	28	3.9	31	
Administered Price Inflation Excluding Exchange Rate Pass-Through and Inertia	1.7	24	1.9	15	
Inertia	0.7	10	0.9	7	
Exchange Rate Pass-Through	2.9	38	5.8	46	
Total	7.7	100	12.5	100	

Figure 3 Interest Rate (over Selic) - 1999:06 - 2003:02 (%p.a. - montlhy average)



We can also verify that there has been a gain in terms of the variability of the inflation rate, output, and interest rate. Table 2 reports the average, standard error and coefficient of variation (ratio of standard error to average) for these variables. It compares the first three and half years of inflation targeting with the Real Plan period before the adoption of inflation targeting. For the earlier period, the table also reports the figures for a shorter sample, which excludes the first quarters of the Real Plan, which were characterized by a transition to stabilization. For the inflationtargeting period, we also consider a shorter sample that excludes the second half of 2002. The inflation rate is measured by the IPCA, output by seasonally adjusted GDP, and the (nominal) interest rate by the Selic rate. We use quarterly data. In the case of GDP, we use the annualized quarter-over-quarter growth rates. The variability of output and the interest rate is lower in the inflation-targeting period. The volatility of inflation in turn is lower if we consider the shorter sample for the inflation-targeting period. This does not imply necessarily that there have been gains in terms of the trade-off between output and inflation because this result also depends on the magnitude and variability of the shocks that hit the economy. On average, output growth is higher and the interest rate is lower in the inflation-targeting period. The inflation rate is lower in the inflation-targeting period if we compare it to the whole period before inflation targeting. In the case of the 1996:01-1999:02 period, the lower average inflation rate is to a large extent a consequence of

the pegged exchange rate regime, which turned out to be unsustainable in the medium run. When the inflation targeting sample ends in 2002:04, the standard deviation of inflation is higher, reflecting the increase in the inflation rate in the last months of that year.

	I	nflation Rate	e		GDP			Interest Rate	•
Period	Average (per year)	Standard Deviation	Coefficient of Variation	Average (per year)	Standard Deviation	Coefficient of Variation	Average (per year)	Standard Deviation	Coefficient of Variation
Real Plan Before									
Inflation Targeting									
1994:4 - 1999:2	10.3	9.2	0.89	2.0	6.3	3.16	35.4	14.1	0.40
1996:1 - 1999:2	5.8	4.8	0.84	2.0	5.2	2.55	28.2	6.0	0.21
Inflation Targeting									
1999:3 - 2002:2	7.1	3.0	0.42	2.4	3.5	1.46	18.0	1.4	0.08
1999:3 - 2002:4	8.9	6.0	0.68	2.5	3.3	1.28	18.2	1.6	0.09

 Table 2

 Average, Standard Deviation and Coefficient of Variation for Inflation Rate, GDP and Interest Rate

 Different Periods (Quarterly Data)

3. Constructing credibility

The success of inflation targeting hinges, to a large extent, on the construction of credibility. Private agents should believe that the central bank will act consistently within the inflation-targeting framework. Gaining credibility, however, takes time. In the context of large shocks, even with a strong response by the monetary authority, expectations will tend to deviate from the targets. In this case, communication with the public so as to explain the reasons of the non-fulfillment of the targets becomes crucial. Furthermore, it is important that expectations converge to the target over a certain time horizon. In this section, we present some evidence on: i) the behavior of the central bank, ii) the behavior of private agents' expectations, iii) the change in inflation dynamics.

3.1. Reaction function of the Central Bank

We estimate a reaction function for the Central Bank of Brazil that relates the interest rate to deviations of expected inflation from the target, allowing also for some interest-rate smoothing and reaction to the output gap and movements of the exchange rate:

$$i_{t} = \mathbf{a}_{1}i_{t-1} + (1 - \mathbf{a}_{1})(\mathbf{a}_{0} + \mathbf{a}_{2}(E_{t}\mathbf{p}_{t+i} - \mathbf{p}_{t+i}^{*}) + \mathbf{a}_{3}y_{t-1} + \mathbf{a}_{4}\Delta e_{t-1}),$$
(1)

where *i* is the Selic rate decided by the Monetary Policy Committee (Copom), $E_{\pi_{t+j}}$ is inflation expectations and π^*_{t+j} is the inflation target, both referring to some period in the future as will be explained below,⁷ y_t is the output gap, and Δe_{t-1} is the nominal exchange rate variation. We use monthly data. Monthly industrial production (seasonally adjusted) measured by IBGE is the proxy for output. The output gap was obtained by the difference between the actual and the HP-filtered series.⁸

We use two sources for inflation expectations. The first one is the inflation forecasts of the Central Bank of Brazil presented in its quarterly *Inflation Report*. The advantage of this source is

⁷ Clarida, Galí, and Gertler (1998, 2000) estimate forward-looking reaction functions for the U.S., Germany, Japan, U.K., France, and Italy. Instead of using central bank or survey expectations, they employ a Generalized Method of Moments (GMM) estimation. The reaction function is basically a forward-looking version of the backward-looking reaction function proposed by Taylor (1993).

⁸ Estimations using output growth and output gap obtained by extraction of a linear trend were also performed. The results were similar and are not reported in this paper.

that the Copom should make interest rate decisions based on its own inflation forecasts. The forecasts in the *Inflation Report* are made assuming a constant interest rate equal to the one decided in the previous Copom meeting. Therefore, they signal whether the Central Bank should change the interest rate.⁹ The second source is obtained from a daily survey that the Central Bank conducts among financial institutions and consulting firms.¹⁰ The survey asks what firms expect for year-end inflation in the current and in the following years.¹¹

The Brazilian inflation-targeting regime sets year-end inflation targets for the current and the following two years. Since it is necessary to have a single measurement of the deviation of inflation from the target, we have used a weighted average of current year and following year expected deviation of inflation from the target, where the weights are inversely proportional to the number of months remaining in the year.¹²

Tables 3 and 4 report the estimations using the Central Bank's inflation forecasts (sample 1999:07-2002:12) and the market forecasts (sample 2000:01-2002:12), respectively.¹³ We present three specifications: the first includes only the deviation of expected inflation from the targets, the second one adds the output gap term, and the third includes also the 12-month exchange rate change. When relevant, we also compare the results to an estimation with sample ending in 2002:06 (not shown).

The first noteworthy result is the high degree of interest-rate smoothing. The coefficient on the lagged interest rate is between 0.7 and 0.9. Most importantly, the point estimates of the coefficient on inflation expectations are greater than one and significantly different from zero in all specifications. Moreover, in the case of the estimations with market inflation expectations, the coefficient is statistically greater than one, with point estimates around 2.0-2.3 (the p-values for the test that the coefficient is equal to 1 are 0.012, 0.040, and 0.053 in specifications I, II, and III, respectively).¹⁴ In the case of central bank expectations, the values are less stable across specifications (from 2.7 to 5.7).¹⁵ The estimated coefficient is significantly different from 1 or close to that (the p-values for the test that the coefficient is equal to 1 are 0.150, 0.101, and 0.058 in specifications I, II, and III, respectively). Therefore, we can conclude that the Central Bank has been reacting strongly to expected inflation. It conducts monetary policy on a forward-looking basis, and responds to inflationary pressures.

¹¹ In November 2001 the survey started collecting expectations for the following 12 months as well.

¹² $D_j = \frac{(12-j)}{12} (E_j \boldsymbol{p}_t - \boldsymbol{p}_t^*) + \frac{j}{12} (E_j \boldsymbol{p}_{t+1} - \boldsymbol{p}_{t+1}^*)$, where D_t is the measure of expected deviation of inflation from the

⁹ Public information about the Copom's inflation forecasts is available only on a quarterly basis. In order to obtain monthly figures, it was necessary to interpolate the data.

¹⁰ This survey is available at the Central Bank of Brazil website (www.bcb.gov.br). In this estimation, we use the inflation expectations collected on the eve of Copom meetings, avoiding possible endogeneity problems.

target, *j* indexes the month, and *t* indexes the year. Observe that D_t does not contain inflation expectations referring to two years in advance, despite the existence of a target for such period. Given the shorter lags in the transmission mechanism of monetary policy estimated for the Brazilian economy and the higher uncertainty associated with the forecasts, it is reasonable to assume the Copom concentrates on current and following year forecasts when making interest rate decisions.

¹³ The data on market expectations for the IPCA are available only as of January 2000.

¹⁴ Favero and Giavazzi (2002) have also estimated a similar reaction function using the market expectations for a shorter sample. They have found a coefficient equal to 1.78. Silva and Portugal (2002) have found different results using a different specification. They have compared the inflation-targeting period with the period of stabilization before inflation targeting, using in the regression a one-month ahead expected inflation obtained with an autoregressive estimation.

¹⁵ If we compare to a sample that ends in 2002:06, the point estimates in that shorter sample are similar when using market's expectations, and are lower in the case of central bank's expectations, although not statistically different.

	Coefficients and standard errors			
Regressors -	Ι	Π	III	
Constant	1.65 (1.08)	3.06* (1.59)	3.80** (1.57)	
Interest Rate (t-1)	0.90*** (0.06)	0.82*** (0.09)	0.77*** (0.09)	
Inflation Rate Expectations (deviations from the target)	5.70* (3.20)	3.54** (1.51)	2.71*** (0.87)	
Output Gap (t-1)		-0.36* (0.21)	-0.18 (0.19)	
Exchange Rate (t-1) (twelve-month change)			0.05* (0.03)	
R-squared	0.9129	0.9160	0.9251	
Adjusted R-squared	0.9084	0.9094	0.9170	
LM Test for Autocorrelation of Residuals (p-values)				
1 lag	0.7853	0.7210	0.7543	
4 lags	0.6831	0.5298	0.5025	

Table 3 Estimation of Reaction Function of Central Bank Using Central Bank's Inflation Expectations Dependent Variable: Selic Interest Rate Target

Notes: Standard error in parentheses. *. ** and *** indicate the coefficient is significant at the 10%. 5%. and 1% level, respectively.

	Coefficients and standard errors			
Regressors	Ι	II	III	
Constant	4.58*** (1.52)	5.38** (2.07)	5.24** (2.12)	
Interest Rate (t-1)	0.71*** (0.09)	0.67*** (0.12)	0.67*** (0.12)	
Inflation Rate Expectations (deviations from the target)	2.32*** (0.53)	2.09*** (0.53)	2.05*** (0.54)	
Output Gap (t-1)		-0.10 (0.15)	-0.07 (1.67)	
Exchange Rate (t-1) (twelve-month change)			0.01 (0.03)	
R-squared	0.9205	0.9214	0.9219	
Adjusted R-squared	0.9157	0.9140	0.9118	
LM Test for Autocorrelation of Residuals (p-values)				
1 lag	0.6586	0.6411	0.5794	
4 lags	0.5362	0.3991	0.4150	

Table 4 Estimation of Reaction Function of Central Bank Using Market's Inflation Expectations Dependent Variable: Selic Interest Rate Target

Notes: Standard error in parantheses. *, ** and *** indicate the coefficient is significant at the 10%, 5%, and 1% level, respectively.

The coefficient on output gap has the wrong sign, but it is statistically significant only in one of the specifications. One possible explanation for the negative sign is that part of the supply shocks that hit the economy led to an increase in inflation and simultaneously to a reduction in output. This clearly occurred in the case of the rationing in electricity. Since we observe a simultaneous interest rate increase and reduction of output, if the inflation expectations term does not capture this change completely, we tend to obtain negative coefficients for the output gap term. Furthermore, note that when we include the exchange rate the coefficient becomes not significant. External shocks tend to generate inflationary pressures at the same time that tend to decrease output, at least in the short run.

3.2. Inflation expectations and the role of the targets

Since mid-2001, 12-month inflation has been above the upper limit of the target tolerance interval.¹⁶ A naive analysis of the inflation-targeting regime in Brazil might say that this regime has not been successful in controlling inflation. Nevertheless, inflation outcomes are not a sufficient statistic to evaluate the performance of the Central Bank given the magnitude of the supply shocks. The evolution of inflation expectations, and the role of the target are also relevant variables in assessing the credibility of the Central Bank.

In the context of significant shocks, it is crucial that private agents understand that, even with a monetary policy consistent with the inflation-targeting framework, actual inflation may breach the targets. Given the magnitude of the shocks that hit the Brazilian economy, a strong reaction of the monetary authorities cannot avoid an increase in the inflation rate and some departure of inflation expectations from the original targets. In terms of inflation expectations, it is important is that they converge to the targets over a certain time horizon.

Two conditions are necessary to guarantee inflation expectations will remain under control. The first is that the conduct of monetary policy should be consistent with the main guidelines expressed by the Copom. In this sense, the reaction function estimated in the previous subsection shows that the Central Bank has been acting consistently within the inflation-targeting framework. The second condition for controlling expectations is clear communication with the public. It is important that private agents understand why actual inflation was above the target and how monetary policy is being conducted in order to drive inflation back to the target. The Central Bank of Brazil communicates with the market via informal speeches and formal documents, such as the minutes of the Copom meetings, which are released one week after the meetings, and the *Inflation Report*, which is published on a quarterly basis. Furthermore, the reasons for the non-fulfillment of the inflation targets in 2001 and 2002 were thoroughly explained in open letters to the Minister of Finance.

The conduct of monetary policy has been based on accommodating the first-round effects of supply and cost-push shocks. This means monetary policy will allow relative price movements to affect inflation, but will neutralize the second-round effects. The Central Bank has developed a methodology that calculates the inflationary impact of current supply shocks as well as the secondary impact of past shocks (due to inertia in the inflation process). Since the primary effect is accommodated, the optimal inflation path may imply that 12-month ahead inflation is above the previous annual target. Therefore, in this situation, given that the Central Bank is no longer aiming for the previous inflation target, it uses an "adjusted target". More specifically, the original target is adjusted in order to take into account the primary effects of the change in relative prices and of past inertia that will be accommodated. Part of inertia is accommodated because the Central Bank also takes output volatility into account in its decisions. The new target is publicly announced.¹⁷

¹⁶ The targets are established only for year-end inflation. We have calculated targets for the other months of the year using linear interpolation.

¹⁷ The adjusted targets for 2003 and 2004, 8.5% and 5.5%, were published in the open letter from the Governor of the Central Bank to the Minister of Finance on 1/21/03 (Banco Central do Brasil, 2003). For a more detailed explanation of the methodology, see Freitas, Minella, and Riella (2002).

transparency and communication are more significant. Private agents know the target the Central Bank is pursuing. Actually, keeping the old target would affect the credibility of the Central Bank because it could be considered unattainable.

Figure 4 shows the 12-month ahead inflation that is expected by the market, the 12-month ahead target, and the actual 12-month accumulated inflation.¹⁸ It is clear that inflation expectations remained below the upper limit of the tolerance interval prior to the last quarter of 2002. This is true even since the second half of 2001, when actual inflation surpassed the tolerance interval. The correlation coefficient between the actual and expected inflation series has increased. From 2000:1 to 2002:1, the correlation is 0.22, but with the sample ending in 2002:12, the value is 0.74. As the graph shows, since mid-2000, the 12-month ahead inflation expectations have been below the actual 12-month inflation. This indicates that private agents tend to expect that the rise in the inflation rate will tend to reverse in the medium run. The fact that actual inflation has been above the value that was expected 12 months ago reflects basically the frequent and large cost-push shocks that hit the economy during this period. It is noteworthy that the difficulties the country faced last year impacted inflation expectations more significantly only in the last quarter of 2002. The median of inflation expectations for 2002 leveled out at around 4.5% through September, but then rapidly deteriorated afterwards and reached 11% at the end of December. The increase in expectations is associated with the expected inflationary effects of the strong exchange rate depreciation and the uncertainties about the future stance of monetary policy under the new government. It does not seem to reflect lack of credibility of the conduct of monetary policy during the period, but uncertainty about its maintenance in the near future.





Another source of evidence suggesting Central Bank gains in credibility comes from evaluation of the role of the targets in expectations formation. We have run OLS regressions of 12-month ahead market inflation expectations on its own lags, the 12-month ahead inflation target, the interest rate, and 12-month inflation rate (sample 2000:01-2003:02). Table 5 reports the results for this specification in column I. All coefficients are statistically significant and have the expected sign. The positive coefficient on the interest rate may be explained by the reaction of interest rates to inflationary pressures. When facing a large supply shock, the central bank raises the interest rate. However, the inflationary effects are not completely eliminated because of three reasons: i)

¹⁸ We estimate the 12-month ahead expected inflation rate using the expected inflation for the remaining months of the current year and, for the remaining months necessary to achieve 12 months, the corresponding proportion of expected inflation for the following year. The 12-month ahead target is estimated by interpolation.

presence of lags in the monetary policy transmission mechanisms; ii) the Central Bank also takes output volatility into account in its decisions; and iii) the Central Bank has acted so as to accommodate first order effects of the change in relative prices (and neutralize second-order effects). As a result, we observe that interest rate and inflation expectations move in the same direction. Since the Central Bank reacts to its own expectations of inflation, interest rate movements also reflect the central bank's inflation expectations.

	Coefficients and standard errors					
Regressors	Ι	Π	Ш	IV		
Constant	-7.35*** (2.33)	-7.33*** (2.32)	-6.22** (2.30)	-6.33** (2.33)		
Market Inflation Rate Expectations (t-1)	0.91*** (0.18)	0.86*** (0.19)	0.89*** (0.18)	0.86*** (0.19)		
Market Inflation Rate Expectations (t-2)	-0.80*** (0.17)	-0.72*** (0.19)	-0.62*** (0.19)	-0.60*** (0.20)		
Interest Rate (t-1)	0.24** (0.12)	0.19 (0.13)	0.18 (0.12)	0.15 (0.12)		
Inflation Rate Target (12-Month Ahead)	1.06*** (0.33)	1.22*** (0.36)	0.92*** (0.32)	1.01** (0.37)		
12-Month Inflation Rate (t-1)	0.45*** (0.15)	0.46*** (0.15)	0.35** (0.15)	0.37** (0.16)		
12-Month Exchange Rate Change (t-1)		0.01 (0.01)		0.01 (0.01)		
Embi Plus Brazil (t-1)			0.06* (0.03)	0.05 (0.03)		
R-squared	0.9148	0.9186	0.9247	0.9255		
Adjusted R-squared	0.9007	0.9017	0.9091	0.9069		
LM Test for Autocorrelation of Residuals (p-values) 1 lag	0.2403	0.25875	0.5061	0.5465		
4 lags	0.3869	0.2711	0.1725	0.0540		

Table 5 Estimation of Inflation Expectations Dependent Variable: Market Inflation Rate Expectations - 2000:1 - 2003:2

Notes: Standard error in parentheses. *, ** and *** indicate the coefficient is significant at the 10%, 5%, and 1% level, respectively.

Most importantly, expected inflation reacts significantly to the inflation targets (coefficient around 1). One could consider that this result could be a consequence of some correlation between targets and past inflation, but note that the regression also includes the actual 12-month inflation rate. Therefore, there are indications that the inflation targets play an important role for expectations. The past inflation term, however, has a statistically significant coefficient, indicating that past inflation still plays a role. It is interesting to note that, if we estimate the same regression with the sample ending in 2002:09, the past inflation term is not significant. Figure 5a shows the recursive estimation for the coefficient on the past inflation term. It started increasing at the end of 2001. We can consider that there are two reasons for this behavior. First, when the economy is hit by a significant inflationary shock, this tends to raise inflation expectations. Second, in the last months of 2002 and beginning of 2003, when the recursive estimates present higher growth, private agents assigned some non-trivial probability to monetary policy under the future government being less strict on inflation. Since the economy was being hit by inflationary shocks, private agents tended to consider that the inflationary effects of these shocks would be more persistence over time. As a result, we observe a higher weight on past inflation in their expectations. Specifications II, III, and IV also include the 12-month exchange rate change and the EMBI Plus for Brazil. For a sample ending in 2002:09 (not shown), the EMBI Plus is not statistically significant, but with the extended sample it becomes significant, possibly reflecting the effect of the confidence crisis of end-2002.

Although the exchange rate change is not statistically significant, we show its recursive estimates in Figure 5b, which rise at the end-2002.



The particularity of the transition period to the new government is clear when we estimate the four specifications with a sample ending in September 2002, and forecast inflation expectations for the following five months. Figure 6 shows these out-of-sample forecasts. All of them point to an increase in inflation expectations, but are significantly below actual inflation expectations, in spite of a adjusted R-squared greater than 0.90.



Since November 2001, the Central Bank has published 12-month ahead inflation expectations, which is recorded in Figure 7. In the estimations we have used so far, we have employed a weighted average of the expectations for the end of the current and following years. We can see that inflation expectations have reverted since the beginning of 2003.

In summary, although the actual inflation rate has been above the upper limit of the tolerance interval in 2001 and 2002, the inflation-targeting regime has been successful in anchoring expectations. This is a consequence of the credibility gains that the Central Bank has achieved since the implementation of the inflation-targeting regime. Only in the fourth quarter of 2002 did inflation

expectations depart from the targets as a result of the confidence crisis. Credibility, however, is still under construction as it takes time to achieve.



Figure 7 12-Month Ahead Inflation Expectations (%p.a.)

3.3. Change in inflation dynamics

As the inflation-targeting regime is supposed to affect the formation of inflation expectations, we can consider the possibility that the backward-looking component of price adjustments has become less important. The share of backward-looking firms could have become smaller and/or firms could place less weight on past inflation when adjusting prices. This would reduce the degree of persistence in inflation. Following Kuttner and Posen (1999), we estimate a simple aggregate supply curve for the low inflation period to assess if the inflation-targeting regime was accompanied by some structural change.¹⁹ Using monthly data, we regress the inflation rate (measured by the IPCA) on its own lags, the unemployment rate²⁰ (lagged one period), and the exchange rate change in 12 months (lagged one period). The sample starts in 1995:07 and ends in 2002:12.²¹ The regression also includes dummy variables that multiply some of the mentioned regressors for the inflation-targeting period. The inflation rate and exchange rate change are measured in monthly terms.

Table 6 shows a specification that includes only one lag for inflation, and another that includes two. It is important to stress two aspects of the estimation. First, dummies for the inflation targeting period that multiply unemployment and the exchange rate do not enter significantly; therefore, they were excluded from the estimation. Second, we have included a dummy variable that assumes the value of one for the last three months of 2002. Without adding this dummy, the residuals in both specifications present serial correlation. Actually, the end of 2002 is a very peculiar period, which it is difficult to be fitted by a simple Phillips curve. Figure 8 shows monthly inflation since 1994. It is evident the change that took place in the mentioned period.

¹⁹ It is important to stress that the structural model of the Central Bank used for inflation forecasting employs quarterly data, and has a different specification: for example, it includes a forward-looking term for inflation, and a term for output gap instead of unemployment rate.

²⁰ We use seasonally adjusted unemployment rate (criterion seven days) produced by IBGE. The results are qualitatively similar if we use the raw data or the unemployment rate estimated according to the criterion of thirty days. ²¹ Since exchange rate change refers to the 12-month change, the sample starts 12 months after the start of the

Barrossor	Coefficients and standard errors			
Regressors	I	II		
Constant	0.65* (0.36)	0.70* (0.36)		
Dummy constant ¹	0.34*** (0.12)	0.51*** (0.14)		
Inflation rate(t-1)	0.56*** (0.11)	0.62*** (0.15)		
Inflation rate(t-2)		-0.09 (0.14)		
Dummv inflation rate (t-1) ¹	-0.46*** (0.17)	-0.43** (0.19)		
Dummv inflation rate (t-2) ¹		-0.35* (0.20)		
Unemployment (t-1)	-0.08 (0.05)	-0.09* (0.05)		
Exchange rate change (t-1) (twelve-month average)	0.08* (0.04)	0.09** (0.04)		
Dummv 2002O4 ²	1.42*** (0.26)	1.47*** (0.25)		
R-squared	0.5593	0.6022		
Adjusted R-squared	0.5271	0.5624		
LM Test for Autocorrelation of Residuals (p-values) 1 lag	0.6646	0.7022		
4 lags	0.2218	0.3599		

Table 6 Estimation of Aggregate Supply Curve Dependent Variable: Monthly Inflation Rate - 1995:08 - 2002:12

Notes: Standard error in parentheses. *, ** and *** indicate the coefficient is significant at the 10%, 5%, and 1% level, respectively. Since exchange rate change refers to the 12-month change, the sample starts in 1995:07 to avoid the inclusion of data b 1Dummy has value one in the inflation-targeting period (1999:06-2002:12), and zero otherwise. It multiplies the associated variable. 2 Dummy has value one in 2002:10 - 2002:12, and zero otherwise.



Figure 8 IPCA - Monthly Change - 1994:09 - 2002:12

From the estimated coefficients on the dummy variables in both specifications, we can conclude there is a statistically significant change in the constant and in the coefficient on lagged inflation in the inflation-targeting period. The point estimate of the autoregressive coefficient in specification I falls from 0.56 to 0.10 in the inflation targeting period (0.56 minus 0.46). This estimation indicates that there has been a substantial reduction in the degree of inflation persistence after inflation targeting was adopted. This implies a lower output cost to curb inflationary pressures and to reduce average inflation.²² Using recursive estimation for the lagged coefficient, however, we do not observe a reduction in the coefficient. We have also used time-varying coefficient estimation for the simple aggregate supply equation. We regress the inflation rate on its own lag, the unemployment rate, and the exchange rate change, setting the coefficient on the lagged inflation as time varying. The filtered values for the coefficient are drawn in Figure 9. We can see a decreasing tendency for the coefficient, except for the last months of 2002, when it rises rapidly.



The coefficient on lagged unemployment is negative and statistically significant or close to that. Its p-values are 0.130 and 0.068 in specifications I and II, respectively. Since the coefficient value is about -0.08, a one-percentage point increase in the unemployment rate decreases the inflation rate by 1.0 percentage points when measured in annual terms. Considering the indirect effects via inflation inertia, the total effect on inflation over a year is 1.95 p.p. and 1.06 p.p. for the whole sample and for the inflation-targeting period, respectively (the periods have different degrees of inflation persistence).

The exchange rate change also enters significantly. The coefficient is around 0.08, which, considering the lagged inflation term, generates a 12-month pass-through of 18% and 9% for the whole sample and for the inflation-targeting period, respectively. As in the unemployment case, the smaller pass-through in the recent period is a consequence of the lower degree of persistence in inflation. However, using a recursive estimation for the coefficient on the exchange rate change, we observe a decline in the pass-through with the adoption of the floating exchange regime in January 1999 (Figure 10). This result is in line with those in Muinhos (2001), which shows a structural

 $^{^{22}}$ Note that, although the constant in the regression is higher in the inflation-targeting period, the unconditional expected inflation (up to a constant referring to the natural unemployment rate) is equal to 1.5 and 1.1 for the periods before and after inflation-targeting adoption using the first specification, and 1.5 and 1.0 employing the second specification.

break in the pass-through coefficient when the exchange rate regime changed. The estimations in that paper are conducted using a linear and a non-linear Phillips curve. The pass-through in the same quarter of the exchange rate change fell from more than 50% to less than 10%. In the following section, we present some estimation for the pass-through using a VAR model and the structural model.



4. Exchange rate changes and pass-through

Dealing with exchange rate volatility has been one of the main challenges to the inflationtargeting regime in emerging markets economies. Compared to industrialized economies, emerging markets seem to be more sensitive to the effects of financial crises than other countries. Exchange rate market volatility generates frequent revisions of inflation rate expectations and may result in non-fulfillment of inflation targets. As a general rule, the actions of the central bank should not move the exchange rate to artificial or unsustainable levels. Nevertheless, the central bank may react to exchange rate movements to curb the resulting inflationary pressures and to reduce the financial impact on dollar denominated assets and liabilities on firms' balance sheets.

Regarding the financial problems associated with exchange rate volatility, Haussmann, Panizza and Stein (2001) have argued that all countries that are not able to issue debt in their own currency are more vulnerable to the impact of currency mismatches in their balance sheets. Those mismatches are even more dramatic in a financially integrated world, where rumors of financial problems may lead to capital flight that might produce self-fulfilling crises, generating a bad equilibrium. As observed by Schmidt-Hebel and Werner (2002), the level of reserves works as insurance against the occurrence of this bad equilibrium. If all the burden of the adjustment to capital outflows during financial crisis is supported by exchange rate depreciation, the country might have a backward bending exchange rate supply curve with no equilibrium being possible. They justify foreign exchange rate intervention based on the following reasons: (i) facilitate adjustment to sudden reductions in capital inflows; (ii) accumulate reserves; (iii) reduce excessive exchange rate volatility (associated with lower liquidity in foreign exchange markets); and (iv) raise the supply of exchange rate insurance.

Given the problems associated with exchange rate volatility and the pros of intervention, the Central Bank of Brazil, like those in other emerging markets economies, including some that have also adopted inflation targeting, has actually been implementing a dirty-floating exchange rate policy.²³ Interventions are made as transparent as possible in order to avoid the concern expressed by Mishkin (2000) that intervention may hinder the credibility of monetary policy as the public may realize that stabilizing the exchange rate takes precedence over promoting price stability as a policy objective.

In Brazil, the volatility of the exchange rate has been considerable. From 1999:07 through 2002:12, the exchange rate (monthly average) depreciated on average 1.8% per month, with a standard error of 4.2 and a coefficient of variation (ratio of standard error to average) of 2.4. The inflationary pressures resulting from exchange rate depreciation are more related to the magnitude of the depreciation than to the pass-through coefficient.²⁴ According to the structural model of the Central Bank, the pass-through to market prices inflation, as a percentage of the observed depreciation, is 12% after one year of the depreciation. The pass-through to administered prices is estimated to be 25%, resulting in a pass-through of about 16% for the headline IPCA. In line with these estimates, between January 2001 and December 2002, the price of the dollar moved from R\$ 1.95 to R\$ 3.64, implying an increase of 86.7%. In the same period, IPCA rose 21.2%. In this sense, Brazil seems to be closer to the lower end of the estimates done by Haussmann, Panizza and Stein (2001). They estimated the pass-through accumulated in 12 months for more than 40 countries and found a value below 5% for G-7 countries, and, on the other extreme, figures above 50% for countries like Mexico, Paraguay and Poland.

We can also use a VAR estimation with monthly data to assess the pass-through and the importance of exchange rate shocks to the variability of inflation. We use two specifications. Both include output, the spread of EMBI+ (Emerging Markets Bond Index Plus) over Treasury bonds.²⁵ the exchange rate (monthly average), and the interest rate (Selic rate - monthly average). Output is measured by seasonally-adjusted industrial production. The inclusion of the EMBI+ was necessary because it is a good indicator for financial crises, both foreign crises (Mexico, Asia, Russia, Argentina) and domestic (beginning of 1999), which have an important impact on interest rates. In the first specification, we use administered and market prices as variables, whereas in the second we use the consumer price index (IPCA) instead. We estimate the model in levels, that is, using I(1) and I(0) regressors instead of using the error correction representation.²⁶ The estimation is consistent and captures possible existing cointegration relationships (Sims, Stock, and Watson, 1990; Watson, 1994). The variables used are the log-levels of output, administered prices, market prices. IPCA and the exchange rate, and the levels of the EMBI+ spread and the interest rate.²⁷ We use a Cholesky decomposition with the following order in the first specification: output, administered prices, market prices, EMBI+, exchange rate, and interest rate. In the second specification, the consumer price index substitutes for administered and market prices. Since the financial variables react more rapidly to shocks, we include them after output and price. We also conduct the estimate using the interest rate before the exchange rate. The results are very similar. The sample includes all the period of the Real Plan, from September 1994 through December 2002.²⁸ In order to capture possible changes in the second semester of 2002, we also estimate the impulse responses using a sample that ends in 2002:06.

Figure 11 shows the impulse responses to a one standard deviation of exchange rate shock. It presents the point estimates for the samples ending in June 2002 and December 2002, and the

²³ Calvo and Reinhart (2002) discuss the limited empirical evidence of truly free-floating countries.

²⁴ See Goldfajn and Werlang (2000) for the reasons for the low pass-through in the Brazilian January 1999 devaluation episode.

²⁵ We use EMBI from Sept./1994 through Dec./1998, and EMBI+ after that.

²⁶ According to augmented Dickey-Fuller unit root tests, we can accept the presence of a unit root for the log-levels of IPCA, administered prices, market prices, exchange rate, interest rate, and for the level of EMBI+ spread. We reject the presence of unit root for the monthly change of those variables, and for the level of interest rate.

²⁷ The lag length of the VAR estimations was chosen according to Schwarz criterion, but we test for the presence of serial correlation of residuals, and increase the number of lags when necessary to obtain no serial correlated residuals. We have used four lags for both specifications.

²⁸ July and August 1994 were excluded because the price indexes were still "contaminated" by the previous high inflation period. In this case, the start of the sample is adjusted according to the number of lags used.

two-standard-error bands for the former sample, which were estimated using a Monte Carlo experiment with 1000 draws. The values shown are percentage points. We stress two aspects. First, the responses of administered and market prices are positive and statistically significant, and the increase in administered prices is greater than that of market. Second, when the sample includes the last months of 2002, we notice an increase in the responses, but still inside the confidence interval of the June sample, which is a kind of stability test for impulse response. Figure 12 shows the responses in the case of the specification that includes the IPCA instead of the administered and market prices.²⁹ Again we see an increase in the response in the last months of 2002, but still inside the bands of the June sample.



Figure 12 Impulse Responses of Price Level (IPCA) to an Exchange Rate Shock



Using the full sample, the exchange rate increases initially 2.6%, reaching a total of 4.3% in the second month, and starts decreasing after that. The rise of both administered prices and market prices reaches a maximum in the eighth month. The values of the pass-through are presented in Table 7, which records the results for the sample ending in December 2002. We estimate the pass-through as the ratio of the price increase in a 12-month horizon to the value of the exchange rate shock. If we consider the value of the exchange shock in the first month, the pass-through is 32.7% for the administered prices, and 17% for the market prices (19.7% and 7.8%, respectively, if we use

²⁹ The response of price level stabilizes if we consider a 24-month horizon.

the shorter sample, which ends in June 2002). Considering the value of the exchange rate shock in the second month, the pass-through is 22% and 11% (12.1% and 4.8% with the shorter sample). The pass-through for the administered prices is 1.9 higher than that for the market prices (2.5 with the shorter sample). The pass-through to IPCA was estimated at 17.9 and 11.4% (14.1% and 8.4% with the shorter sample), considering the first and second month shock, respectively.

			S	ample			
Value of Exchange Rate	Real Plan Period		Inflat	Inflation-Targeting Period			
Snock Considered	Administered Prices	Market Prices	IPCA	Administered Prices	Market Prices	IPCA	
Pass-Through Using the First Month Exchange Rate Shock	32.9%	17.0%	17.9%	20.0%	11.3%	13.1%	
Pass-Through Using the Second Month Exchange Rate Shock	22.3%	11.0%	11.4%	18.8%	10.3%	11.5%	
Ratio of Pass-Through Administered Prices to Market Prices			1.9			1.8	

Table 7
Pass-Through Considering Different Specifications:
Ratio of Price Change (12-month horizon) to an Exchange Rate Shock

Since the inflation-targeting regime may have represented a structural change in the relationships, and the exchange rate regime is different from the majority of the previous period, we estimate a VAR model for the first three years of inflation targeting (1999:07-2002:12). However, the sample size is too short, and the response of administered and market prices is positive, but not statistically significant using a two-standard-error band (they are significant in the first months if we use a one-standard-error band). To compare with the Real Plan period, however, we show the point estimates in Table 7.³⁰ One can see a decrease in the pass-through specially using the first month exchange rate shock in both administered and market prices³¹. These results using a VAR model are in line with those in the recursive estimation of the aggregate supply curve shown in subsection 3.3 and again in Muinhos (2001).

Therefore, exchange rate volatility is an important source of inflation variability. The design of the inflation-targeting framework has to take into account this issue to avoid that a possible non-fulfillment of inflation targets as a result of exchange rate volatility may reduce the credibility of the central bank.

5. Conclusions

The inflation-targeting regime in Brazil is relatively new, but has shown to be important in achieving low levels of inflation even in a context of large shocks. The presence of a central bank committed to the achievement of pre-announced inflation targets has worked as an important coordinator of expectations and generated a more stable inflation scenario. The pursuit of this goal and the significant increase in transparency that has marked the action of monetary policy have

 $^{^{30}}$ We have used two lags in both specifications. With IPCA and three lags, however, the values are smaller for the pass-through: 9.6% and 4.8%.

³¹ With the sample only until June 2002, all the pass-throughs were smaller, and there was no difference between the Real plan and inflation-targeting periods.

contributed to the development of the awareness of the importance of the commitment to price stability.

During this period, the regime has faced many challenges, including the construction of credibility – which is still a work in progress – the change in relative prices, and exchange rate volatility. Dealing with these challenges has required a large effort by the Central Bank, which itself has also learned substantially and has improved the system. The Central Bank has reacted strongly to inflation expectations, consistent with the inflation-targeting framework. Market expectations have remained under controlled, even in the presence of inflationary shocks. The estimations also indicate a reduction in the degree of inflation persistence.

Even with the confidence crisis in the second half of 2002, the inflation targeting framework supported the burden of the crisis, allowing the nominal exchange rate to adjust and the interest rate to increase to prevent inflation from persisting in high levels in the economy. In view of the intensity and magnitude of the shocks that hit the Brazilian economy in 2001 and 2002, the cost in terms of output losses of a policy aimed at completely offsetting these shocks in a short period of time and keeping inflation within the tolerance intervals would have been significantly higher. The Brazilian experience has been a successful stress test for the inflation targeting framework.

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